Exercise 41

For the following exercises, for each pair of functions, find a. f + g b. f - g c. $f \cdot g$ d. f/g. Determine the domain of each of these new functions.

$$f(x) = 6 + \frac{1}{x}, \ g(x) = \frac{1}{x}$$

Solution

$$f + g = f(x) + g(x) = \left(6 + \frac{1}{x}\right) + \left(\frac{1}{x}\right) = 6 + \frac{2}{x}$$
 Domain: $\{x \mid x \neq 0\}$

$$f - g = f(x) - g(x) = \left(6 + \frac{1}{x}\right) - \left(\frac{1}{x}\right) = 6$$
 Domain: $\{x \mid x \neq 0\}$

$$f \cdot g = f(x)g(x) = \left(6 + \frac{1}{x}\right)\left(\frac{1}{x}\right) = \frac{6}{x} + \frac{1}{x^2}$$
 Domain: $\{x \mid x \neq 0\}$

$$f/g = \frac{f(x)}{g(x)} = \frac{6 + \frac{1}{x}}{\frac{1}{x}} = \frac{6x + 1}{1} = 6x + 1$$
 Domain: $\{x \mid x \neq 0\}$

Note that the domain for any expression is the same regardless of simplification.